

FIG. 1

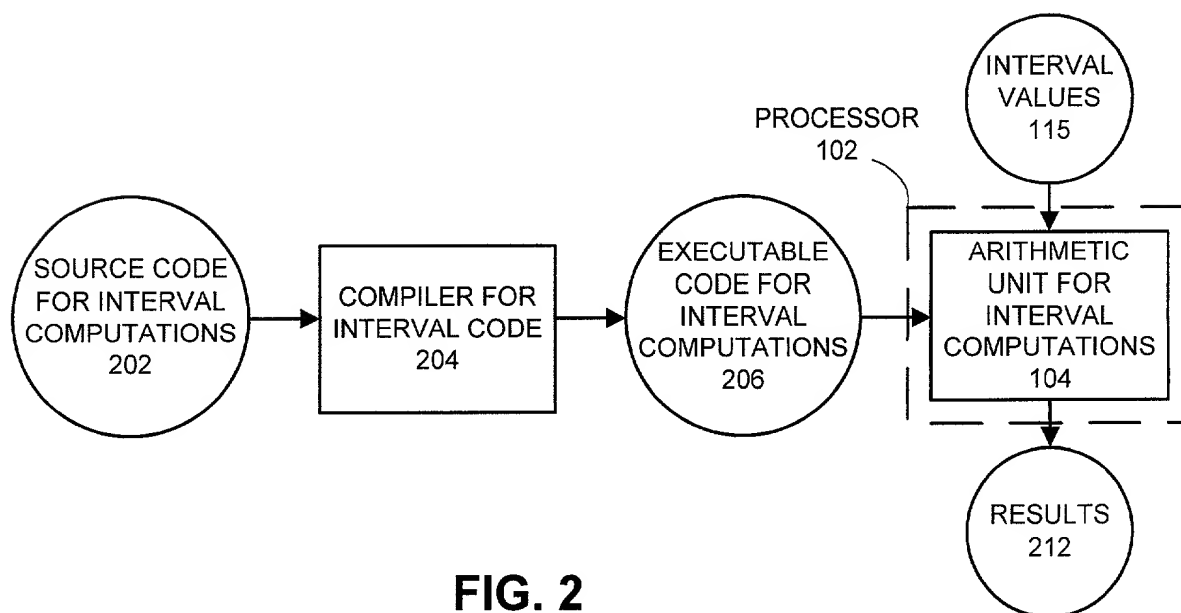


FIG. 2

FIG. 3 is a block diagram of an arithmetic unit for interval computations. The unit 104 receives two intervals, INTERVAL 302 and INTERVAL 312, and outputs two floating point numbers, FIRST FLOATING POINT NUMBER 304 and SECOND FLOATING POINT NUMBER 306, and two floating point numbers, FIRST FLOATING POINT NUMBER 314 and SECOND FLOATING POINT NUMBER 316.

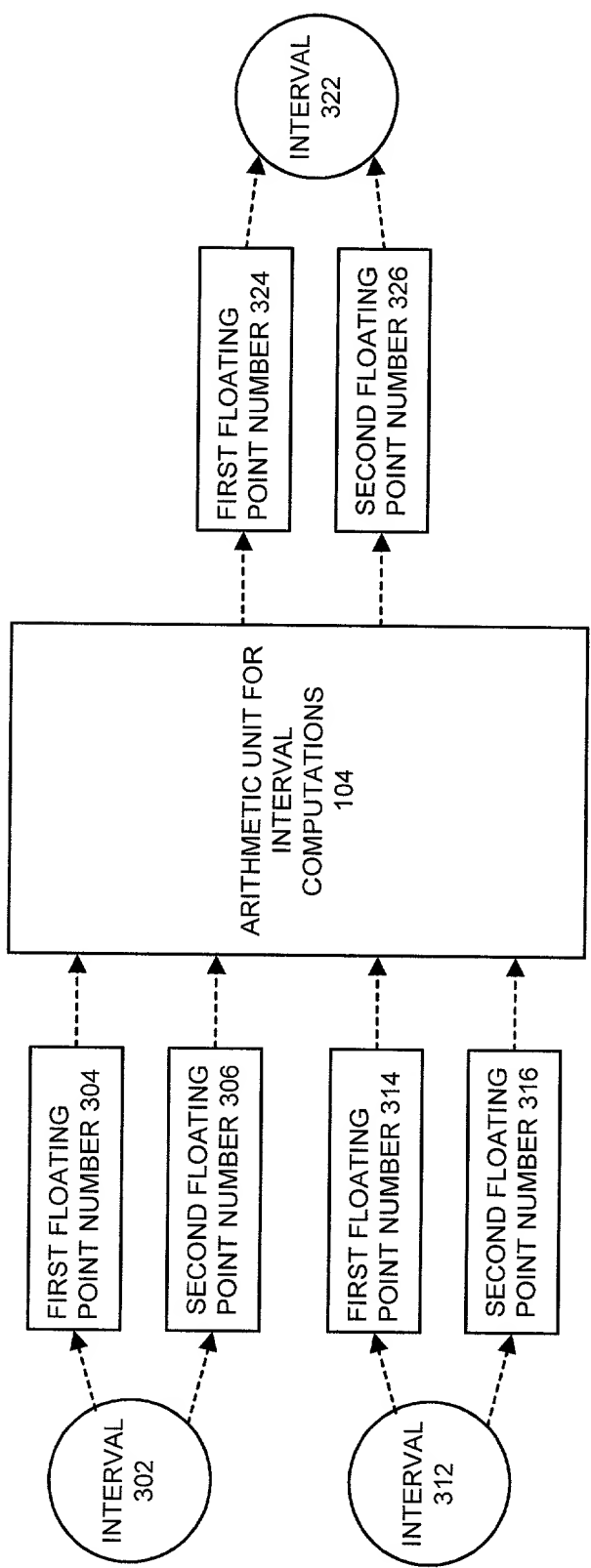


FIG. 3

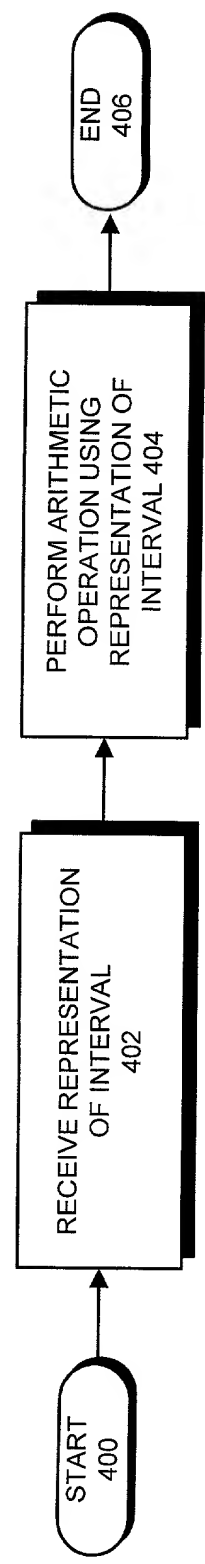


FIG. 4

$$X \equiv [\underline{x}, \bar{x}] \equiv \{x \in \mathfrak{R}^* | \underline{x} \leq x \leq \bar{x}\}$$

$$Y \equiv [\underline{y}, \bar{y}] \equiv \{y \in \mathfrak{R}^* | \underline{y} \leq y \leq \bar{y}\}$$

$$(1) \quad X + Y = [\downarrow \underline{x} + \underline{y}, \uparrow \bar{x} + \bar{y}]$$

$$(2) \quad X - Y = [\downarrow \underline{x} - \bar{y}, \uparrow \bar{x} - \underline{y}]$$

$$(3) \quad X \times Y = [\min(\downarrow \underline{x} \times \underline{y}, \underline{x} \times \bar{y}, \bar{x} \times \underline{y}, \bar{x} \times \bar{y}), \max(\uparrow \underline{x} \times \underline{y}, \underline{x} \times \bar{y}, \bar{x} \times \underline{y}, \bar{x} \times \bar{y})]$$

$$(4) \quad X / Y = [\min(\downarrow \underline{x} / \underline{y}, \underline{x} / \bar{y}, \bar{x} / \underline{y}, \bar{x} / \bar{y}), \max(\uparrow \underline{x} / \underline{y}, \underline{x} / \bar{y}, \bar{x} / \underline{y}, \bar{x} / \bar{y})], \text{ if } 0 \notin Y$$

$$X / Y = \mathfrak{R}^*, \text{ if } 0 \in Y$$

FIG. 5

<u>INTERVAL</u>	<u>REPRESENTATION</u>	
[empty]	$[NaN_{\emptyset}, NaN_{\emptyset}]$	(1)
$[-\infty, +\infty]$	$[-inf, +inf]$	(2)
$\{-\infty, +\infty\}$	$[+inf, -inf]$	(3)
$[-\delta, b], -fp_max \leq b \leq +fp_max$	$[-inf, B]$	(4)
$[a, b], a < b$	$[A, B]$	(5)
$[a, 0], -fp_max \leq a \leq -fp_min$	$[A, +0]$	(6)
$[0, 0]$	$[-0, +0]$	(7)
$[\epsilon, b], +fp_min \leq b \leq +fp_max$	$[+0, B]$	(8)
$[a, -\epsilon], -fp_max \leq a \leq -fp_min$	$[A, -0]$	(9)
$[0, b], +fp_min \leq b \leq +fp_max$	$[-0, B]$	(10)
$[a, +\delta], -fp_max \leq a \leq +fp_max$	$[A, +inf]$	(11)
$[-\infty, b], -fp_max \leq b \leq +fp_max$	$[+inf, B]$	(12)
$[a, +\infty], -fp_max \leq a \leq +fp_max$	$[A, -inf]$	(13)
$[-\infty, a] \cup [b, +\infty]$ $-fp_max \leq a < b \leq +fp_max$	$[B, A]$	(14)

FIG. 6